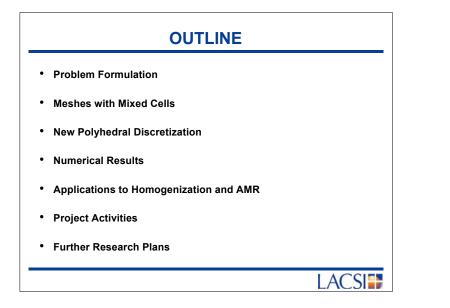


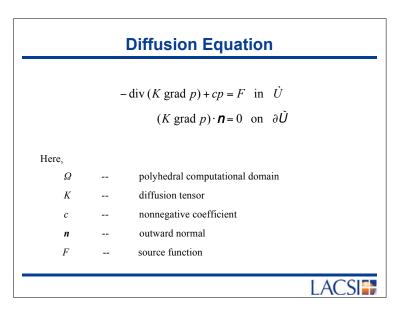
http://lacsi.rice.edu/review/slides_2006

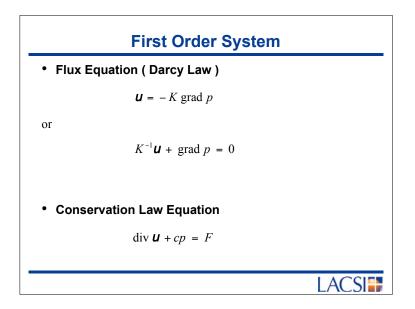
LACSI Review, February 2006

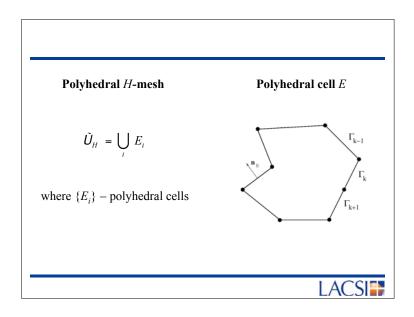
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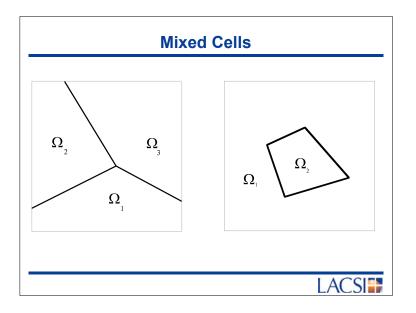
LACSI Project: 2005 Advanced Numerical Methods for Diffusion Equations in Heterogeneous Media on Distorted Polyhedral Meshes LANL: M. Shashkov – PI K. Lipnikov, D. Moulton, S. Runnels UH: Y. Kuznetsov – PI O. Boyarkin – PostDoc V. Gvozdev, D. Svyatskiy – Graduate Students S. Repin – Visiting Research Professor

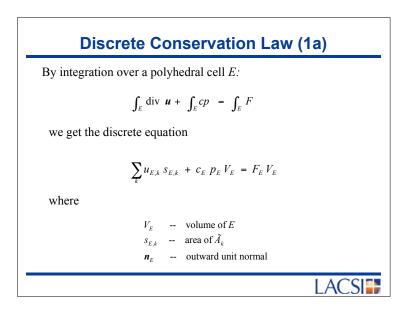


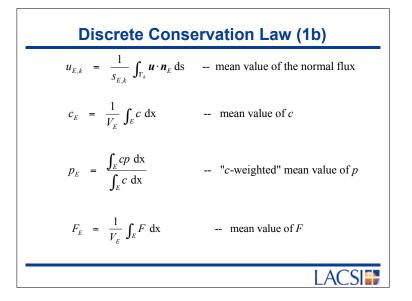


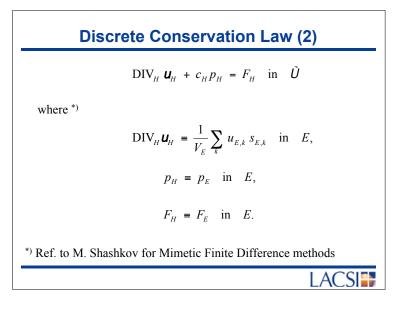


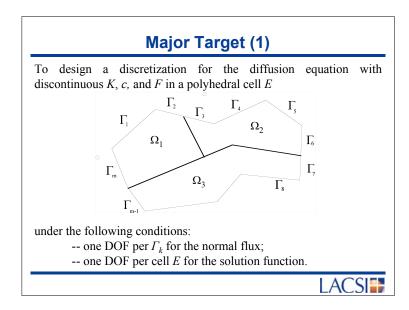


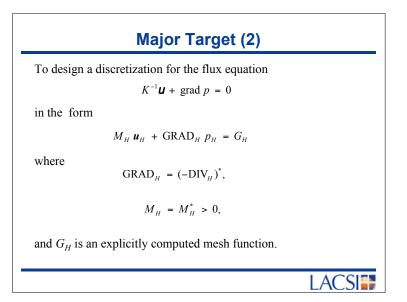












Polyhedral Discretizations 2003/2004

Major assumptions:

$$c_E = \frac{1}{V_E} \int_E c \, dx \approx c \quad \text{in} \quad E$$
$$F_E = \frac{1}{V_E} \int_E F \, dx \approx F \quad \text{in} \quad E$$

Major advantages:

- Arbitrary diffusion tensor
- Arbitrary polyhedral meshes including meshes with nonconvex and degenerated cells
- Nonmatching and AMR polyhedral meshes

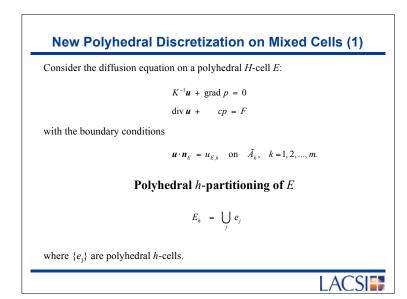
LACSI

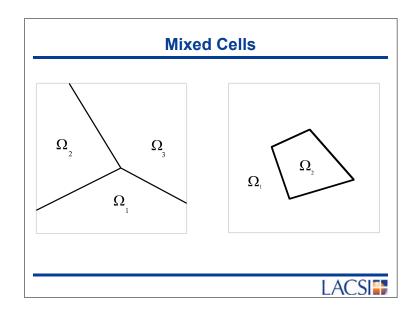
Impact on ASC Projects

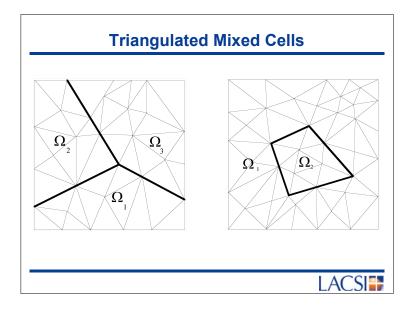
LANL researchers M. Shashkov and K. Lipnikov in T7 group, and S. Runnels in X3 group have recently implemented the proposed polyhedral discretization scheme for the diffusion equations in FLAG code for SHAVANO project.

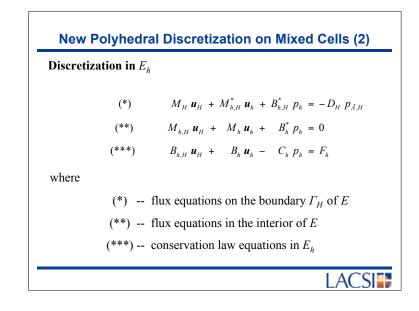
A parallel version of the code was developed by K. Lipnikov and S. Runnels in cooperation with other members of X3 group.

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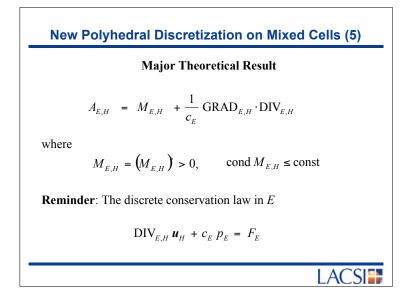


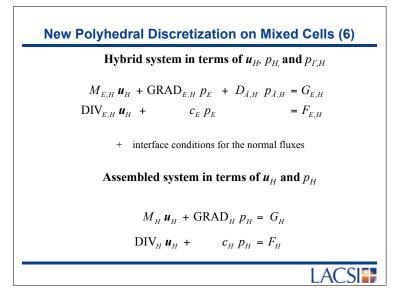


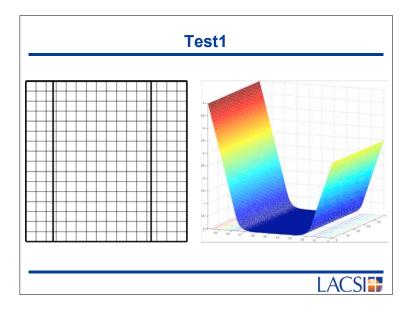


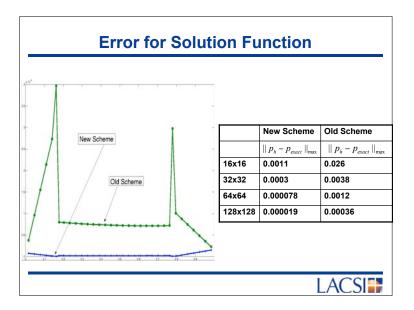
New Polyhedral Discretization on Mixed Cells (3)The mesh operator $L_h = \begin{pmatrix} M_h & B_h^* \\ B_h & -C_h \end{pmatrix} = (L_h)^*$ is nonsingular. Thus, $\begin{bmatrix} \boldsymbol{u}_h \\ P_h \end{bmatrix} = -(L_h)^* \begin{bmatrix} M_{h,H} \\ B_{h,H} \end{bmatrix} \boldsymbol{u}_H + (L_h)^* \begin{bmatrix} 0 \\ F_h \end{bmatrix}$

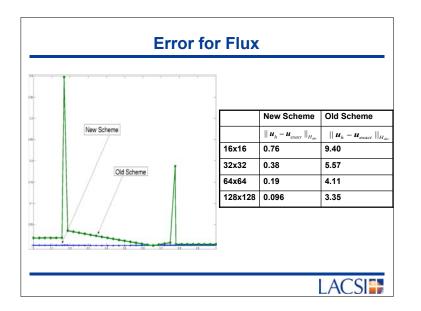
Substituting \boldsymbol{u}_h and p_h in the flux equation on Γ_H we get the equation $\mathcal{A}_{E,H} \boldsymbol{u}_H + D_H p_{\bar{A},H} = \hat{G}_{E,H}$ where $\mathcal{A}_{E,H} = \left[M_{h,H}^* - B_h^* \right] (L_h)^1 \begin{bmatrix} M_{h,H} \\ B_h \end{bmatrix} = (A_{E,H}) > 0$ and $p_{\bar{A},H} = \frac{1}{S_{E,k}} \int_{I_k} p \text{ ds on } \tilde{A}_k, \ k = 1, 2, ..., m.$

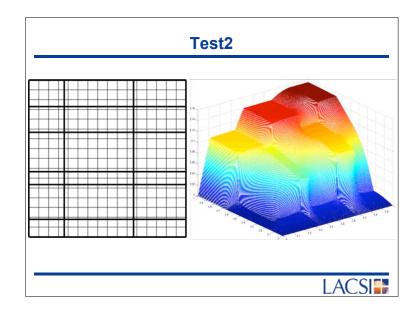


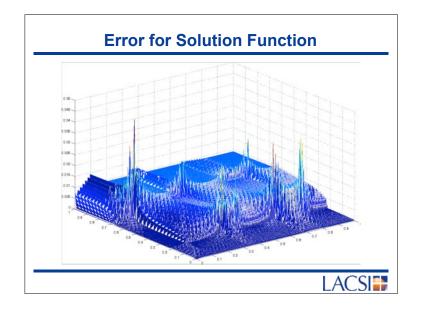


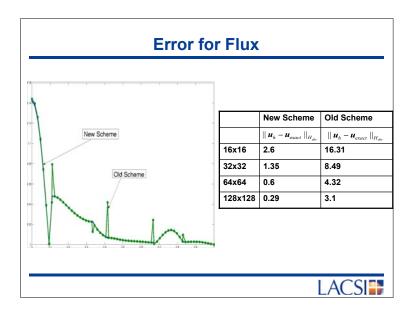


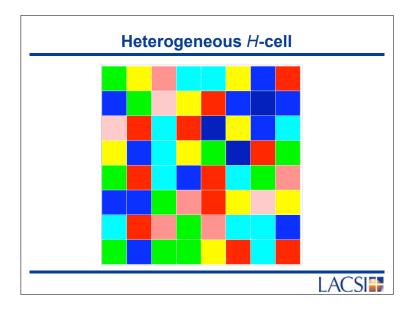


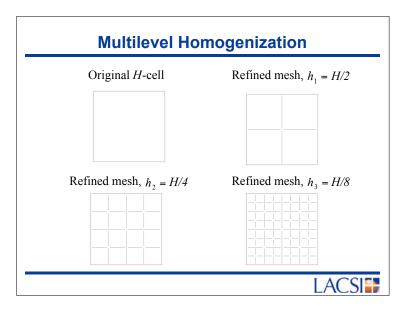


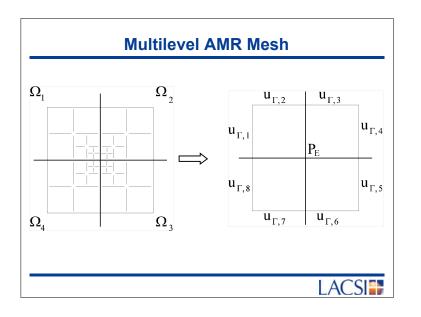












LANL U	H Communication		
 LACSI Symposium, Santa Fe 2005: Workshop on advanced numerical methods for PDEs 			
LANL presentations:	UH presentations:		
K. Lipnikov, T7 D. Moulton, T7 S. Runnels, X3 M. Shashkov, T7 J. Warsa, CCS4	V. Gvozdev – Ph.D. student Y. Kuznetsov D. Svyatskiy – Ph.D. student		
• Meeting at UH, January 11—14, 2006			
Attendees: LANL: M. Shashkov UH: Y. Kuznetsov, O. Boyarkin, D. Svyatskiy			
	LACSI		

Education Issues (1)

Konstantin Lipnikov:

2001 & 2002:	 summer semesters at LANL (Ph.D. Thesis - 2002)
2002 2004:	 PostDoc at T7 group, LANL
since January 2005:	 limited term staff member at T7 group, LANL

Vadim Dyadechko:

2002 & 2003: -- summer semesters at LANL (Ph.D. Thesis – 2003) since September 2003: -- PostDoc at T7 group, LANL

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Further Research Plans

- 3D evaluation of new polyhedral discretizations
- Applications to AMR
- Multilevel preconditioners based on polyhedral discretizations
- Discretizations on anisotropic polyhedral meshes

Education Issues (2)		
Oleg Boyarkin:		
2001—2004:	Graduate Student at UH supported by LACSI	
2004:	Ph.D. Thesis	
since January 2005	: PostDoc at Department of Mathematics, UH	
<u>Daniil Svyatskiy</u> :		
2004 & 2005:	summer semesters at LANL	
Plan:	Ph.D. Thesis – April 2006	
	PostDoc at T7 group, LANL - from June 2006	
	LACSI	

